

Chapter 14 / Example 19

Type I and type II errors

In order to satisfy quality control the mean number of flaws in aluminium sheets must be less than or equal to 0.6 flaws per metre length. A length of 7 m is inspected.

Assuming the number of flaws follows a Poisson distribution:

- a state the distribution of the number of flaws (X) in the length sampled, assuming an average of 0.6 flaws per metre
- b state the hypotheses for the test
- c find the critical region for the test at the 5% significance level
- d find the probability of
 - i a type I error
 - ii a type II error, given the mean is in fact 0.72 flaws per metre.

Press **MENU** 7 **TABLE**.

Press **F5** SET and change the settings so that the table starts from 0 and ends at 20.

Press **EXIT**.

Table Setting
X

Start: 0
End : 20
Step : 1

Press **OPTN** **F6** \triangleright **F3** STAT **F1** DIST **F6** \triangleright **F1** POISSON **F2** Pcd

Enter x as Lower and 100 as Upper and 4.2 as λ , separated by commas. Close the parentheses and press **EXE**.

Table Func : Y=
Y1: PoissonCD(x, 1[—]
Y2: [—]
Y3: [—]
Y4: [—]
Y5: [—]
Y6: [—]
[SELECT] [DELETE] [TYPE] [STYLE] [SET] [TABLE]

Press **F6** TABLE

The function is shown in the table.

X	Y1
0	1
1	0.985
2	0.922
3	0.7897

0

FORMULA DELETE ROW EDIT GPH-CON GPH-PLT

Scroll down the table using **▼**

From the table, $P X \geq 8 > 0.0639$ and $P X \geq 9 > 0.0279$.

The critical region is $X \geq 9$

The probability of a type I error is 0.0279

X	Y1
7	0.1325
8	0.0639
9	0.0279
10	0.0111

8

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Press **MENU** 1 **RUN-MAT** to display the Run-Matrix screen for arithmetical calculations.

Press **OPTN** **F5** **STAT** **F3** **DIST** **F6** **▷** **F1** **POISSON** **F2** **Pcd**

Enter 0 as Lower and 8 as Upper and 5.04 as λ , separated by commas. Close the parentheses and press **EXE**.

$$P(X \leq 8 | p = 5.04) = 0.929$$

This is the probability of a type II error.

PoissonCD(0,8,5.04)
0.929263884

□

Ppd | Pcd | InvP